

Titre de la thèse :

A study of Optimized Spanning Trees and their use in Computer Networks

Host Laboratory :

LIB Laboratory, University of Burgundy, Dijon, France

Speciality :

Computer Science

Keywords :

Spanning tree; Graph ; Optimization; Algorithm; Networks

Job description

Every connected graph containing cycles possesses many spanning trees. Defining and using many spanning trees in a graph or within a network can be of practical interest, for instance in IoT (Internet of Things) mesh, ad-hoc and data center networks [2, 13, 11,17], through improved reliability and Quality of Service (QoS) in these networks in particular if the spanning trees' disjunction is optimized. The spanning trees T_1, T_2, \dots, T_k of a graph G are completely independent spanning trees (CISTs for short) if for every nodes x and y , the paths between x and y in the tree T_i are pairwise vertex disjoint except on their end-vertices.

Since its introduction by Hasunuma in 2001 [8], the problem attracted many research works. The problem of deciding if a graph has two CISTs is NP-complete [9]. Araki [1] provided a Dirac type condition for a graph to have k CISTs. Various authors proved the existence of two or three CISTs in some hypercube variants [14, 4, 16, 3]. On other classes of graphs there are partial results for planar graphs [9], product graphs [10, 6], partial k -trees [12], Cayley graphs [15]. As most of the graphs do not even have two CISTs, Darties et al. [7] introduced a relaxation of the problem by defining (i,j) -ISTs by allowing the spanning trees to share at most i internal nodes and at most j internal edges in total.

The objective of this thesis is to remove several research barriers and to propose innovative solutions. Thus, we specify as research axes the study of optimized CISTs and (i,j) -ISTs on both the theoretical (existence/non-existence proofs), algorithmical (heuristics, parameterized complexity), and practical (usefulness of these structures to address problems in emerging networks such as the Internet of Things as well as 5G and 6G networks) aspects. In particular, possible starting points can be to:

- Find many optimized (i,j) -IST (with small i and/or j) in new graph classes, for instance circulant or Kneser graphs or to optimize the maximum diameter (or mean distance) of the built spanning trees;
- Propose new heuristic methods for finding CISTs or (i,j) -IST in an arbitrary graph and test them on real graphs as well as networks;
- Investigate the use of CISTs and (i,j) -ISTs in the field of networking while considering current and emerging network environments (Internet of Things (IoT), new generations of 5G/6G mobile networks, Cloud Computing/Networking, VANETs, etc.).

Bibliography

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Applicant profile

We are looking for a good candidate (Master's degree, engineer or equivalent in computer science or mathematics) with skills in the fields of graphs and networks:

- Graph theory, Technologies used in networks: TCP / IP architecture, etc.

- Network simulation: NS3/NS2/OMNET ++
- Object-oriented programming: C ++ / Java.

Financing institution : MESRI Etablissement

Application deadline : 1st June 2024

Start of contract : 1st Octobre 2024

Monthly gross salary: 2100€

Thesis Supervisor

Olivier TOGNI, Professeur, Head of the LIB CombNet team, Olivier.Togni@u-bourgogne.fr

Thesis Co-Supervisors

Nader MBAREK, Professor, Deputy Director of the LIB, Nader.Mbarek@u-bourgogne.fr

Mohammed LALOU, Associate Professor, Mohammed.Lalou@u-bourgogne.fr

Applicants are invited to submit their application to the PhD supervisor and co-supervisors listed above. Application must contain the following documents:

- ✓ A detailed CV
- ✓ Cover letter
- ✓ Transcripts and results in Bachelor, Master, or equivalent degrees (while indicating your ranking and the number of students)
- ✓ At least 1 reference letter